Investigation of the prefrontal cortex in response to duration-variable anagram tasks using functional near-infrared spectroscopy

Fenghua Tian  
The University of Pennsylvania  
School of Medicine  
Department of Biophysics and Biochemistry  
Philadelphia, Pennsylvania 19104  
and  
The University of Texas at Arlington  
Department of Bioengineering  
P.O. Box 19138  
Arlington, Texas 76019

Britton Chance  
The University of Pennsylvania  
School of Medicine  
Department of Biophysics and Biochemistry  
Philadelphia, Pennsylvania 19104

Hanli Liu  
The University of Texas at Arlington  
Department of Bioengineering  
P.O. Box 19138  
Arlington, Texas 76019

Abstract. We hypothesize that nonlinearity between short-term anagram tasks and corresponding hemodynamic responses can be observed by functional near-infrared spectroscopy (fNIRS) in the prefrontal cortex (PFC). The PFC of six human subjects in response to anagram tasks is investigated using multichannel fNIRS. Concentration changes of oxyhemoglobin and deoxyhemoglobin in the PFC are measured with variable anagram durations and at two difficulty levels (four- and six-letter anagrams). The durations to perform the selected anagram tasks range from several seconds to more than one minute. The dorsolateral PFC areas exhibit consistent and strong hemodynamic deactivation during and shortly after task execution. The superposition principle of a linear system is employed to investigate non-linear hemodynamic features among three task duration subgroups: D1 = 2.0 sec, D2 = 4.0 sec, and D3 = 8.0 sec. Such analysis shows clear nonlinearity in hemodynamic responses on the PFC with task durations shorter than 4 sec. Our observation of significant deactivation in early hemodynamic responses in the PFC is consistent with multiple fNIRS studies and several reports given in the field of functional magnetic resonance imaging. A better understanding of nonlinearity in fNIRS signals will have potential for us to investigate brain adaptation and to extrapolate neuronal activities from hemodynamic signals.

Keywords: functional near-infrared spectroscopy; prefrontal cortex; anagram; hemoglobin deactivation; nonlinearity.

1 Introduction

Functional near-infrared spectroscopy (fNIRS) has been proposed as a promising technique for hemodynamic imaging of brain activities.1,2 The near-infrared light penetrates the skull and reaches the cortical layer of the brain. It is mainly absorbed by two principal chromophores in tissue, i.e., oxygenated hemoglobin (HbO2) and deoxygenated hemoglobin (Hb) that have significantly different absorption coefficients in the near-infrared region (670 to 900 nm).3 Therefore, by using two or more wavelengths in this region, changes of cerebral HbO2 and Hb concentrations can be quantified. The fNIRS technique measures the hemodynamic signals of the brain similarly to the blood-oxygen-level-dependent (BOLD) signal in functional magnetic resonance imaging (fMRI).4 While the spatial resolution of fNIRS is limited5–7 compared to that of fMRI, the former has a remarkable temporal resolution down to milliseconds and has the advantages of being compact, low cost, and easy to use without complete body confinement. It has been widely accepted by the researchers that fNIRS and fMRI are complementary to one another in brain functional imaging.

Early studies in both fMRI8 and fNIRS9 pointed to a linear relationship between the stimulus parameters (i.e., duration and intensity) and the resultant cerebral, hemodynamic response (BOLD signal in fMRI, HbO2 and Hb concentrations in fNIRS). A linear system model,10 as defined by the principle of superposition with respect to the stimulus duration \[ f(x) = a f(x) + b f(0) \] and of scaling with respect to the stimulus intensity \[ f(a x) = a f(x), \] where \( a \) is a scalar constant, was applied to predict the cerebral response while the stimulus parameter was changed.11–13 However, recent studies in fMRI using various types of stimuli showed that considerable nonlinearity in BOLD signals did exist when utilizing a short period of stimulus (several seconds), and that such nonlinearity varied across cortices. For example, studies looking
at the primary visual cortex reported that the BOLD signal was nonlinear for stimuli less than 4 sec,\textsuperscript{14} or nonlinear for stimuli less than 3 sec,\textsuperscript{15,16} and linear above these durations. Two studies looking at the primary auditory cortex reported that the BOLD signal was nonlinear for stimuli less than 6 sec,\textsuperscript{17} or nonlinear for stimuli less than 10 sec,\textsuperscript{16} and linear above these durations. Soltysik et al.\textsuperscript{16} also reported that the BOLD signal in the primary motor cortex is nonlinear for stimuli less than 7 sec and linear above this duration. While the exact implication of this nonlinear behavior still needs to be further explored, such studies allow us to investigate the neuronal adaptation and other functional properties of neurons within a specific brain region.\textsuperscript{18} Also, knowing the ranges of stimulus duration and rate for the nonlinear response to occur would be useful in the experiment design, such as precluding the use of short intervals between experimental stimuli, etc.

The prefrontal cortex (PFC) is an executive area for cognitive activities that deal with memory, language, and problem solving.\textsuperscript{19–21} A number of studies on the roles of PFC during working memory tasks have been conducted on adults using fMRI,\textsuperscript{22,23} and on adults and children using fNIRS.\textsuperscript{24,25} Most of the higher cognitive functions have shown some use of working memory. Similar studies have also been conducted on infants by Baird et al.\textsuperscript{26} to assess the cognitive maturation of the higher cognitive functions have shown some use of above these durations. Soltysik et al.\textsuperscript{16} also reported that the task durations for the nonlinear response to occur in cognitive cortices exists only within a short stimulus duration, which has not been the focus in most of the previous fNIRS studies. Thus, we conducted a study in the PFC in response to the anagram tasks using a multichannel fNIRS imager. The duration (i.e., the executing time) of the anagram task was variable, ranging from several seconds to more than one minute. This study provided us with a broad view on the variability of the PFC in response to cognitive, problem-solving tasks. We hypothesized that the nonlinear behavior also existed between the short-time stimulus and the fNIRS-derived readings. This hypothesis is based on the fact that the BOLD signal in fMRI and hemoglobin concentrations derived from fNIRS share similar hemodynamic processes occurring in the cortices during brain activities. Specifically, we examined the PFC hemodynamic responses in three discrete subgroups (based on their task durations), and utilized the superposition principle of the linear system model to determine the range and extent of the potential nonlinearity. A better understanding of nonlinearity in fNIRS signals will allow us to investigate brain adaptation and to extrapolate neuronal activities from hemodynamic signals.\textsuperscript{29–31}

## 2 Materials and Methods

### 2.1 Subjects and Cognitive Task

A total of six female subjects (age ranged from 17 to 19 years) were recruited. The subjects were high school juniors or seniors who took part in a summer student minority program on brain function study at the University of Pennsylvania. Written informed consent was obtained from each subject prior to being enrolled.

An anagram task starts from a scrambled word given to the subject (e.g., “e-t-t-x” scrambled from the word “text”), who needs to reorganize the letters to form a correct (real) word. The difficulty level of an anagram task is graded by the number of letters that the word consists of. Before taking the formal test, the subjects were asked to practice demonstrations and decide a task level with moderate difficulty accordingly. In a formal test, ten anagram tasks were presented sequentially on a computer monitor. When a task slide was presented, the subject would manipulate the letters, decided whether or not these letters could be reorganized into a correct word, and then pressed the keyboard to show her judgment (Y for a positive reply and N for a negative reply). The executing time of the task (or duration), defined from the task onset to the following key-stroke entry, was variable. The task slide vanished immediately after the key was hit, followed by a 30-sec rest period, during which three-letter temporary slides were presented on the monitor at a 3-sec interval to maintain the subject’s visual stimuli. On average, one test took about 6 to 10 min. The subject took multiple tests daily with a 30-min break between the consecutive tests. Overall, the experiment lasted for one week; the total number of the tests that each subject completed ranged from 8 to 24.

To evaluate the accuracy of the subjects’ performance, four different types of outcomes, CP, CN, IP, and IN, were defined: CP means that the letters presented could be reorganized into a correct word and the subject also gave a positive judgment. Similarly, CN means that a correct word was given but the subject gave a negative judgment. IP means that an incorrect word was given with a positive judgment. IN means that an incorrect word was given with a negative judgment. In each test, nine out of the total ten tasks were solvable, meaning that the letters in nine out of ten tests could be reorganized into a correct word. Therefore, CP and CN were the majority (90%) of the test outcomes for each subject. The accuracy of each subject’s performance was evaluated as the ratio of CP and IN outcomes (the correct judgments made for both correct and incorrect words) relative to the total tasks she performed throughout the tests.

### 2.2 Principle of Near-Infrared Spectroscopy Imaging

Optical density (OD) is conventionally defined as OD = log\[I_b/I(t)\], where \(I_b\) is the baseline optical intensity and \(I(t)\) is the optical intensity at time \(t\). The principle of continuous-wave NIRS imaging is based on the modified Beer-Lambert law,\textsuperscript{130} in which the relationship between the change in optical density (\(\Delta OD\)) due to light absorption perturbation and the relative changes of \(\text{HbO}_2\) and \(\text{Hb}\) concentrations from baseline can be expressed as:
\[ \Delta \text{OD}(\lambda) = r \cdot \text{DPF}(\lambda) \cdot \{ \varepsilon_{\text{Hb}}(\lambda) \cdot \Delta \text{Hb} + \varepsilon_{\text{HbO}_2}(\lambda) \cdot \Delta \text{HbO}_2 \}, \]

where \( \varepsilon \) is the molar extinction coefficient (\( \mu \text{M}^{-1} \cdot \text{mm}^{-1} \)) of \( \text{HbO}_2 \) or \( \text{Hb} \), \( \Delta \text{Hb} \) and \( \Delta \text{HbO}_2 \) are the changes of \( \text{Hb} \) and \( \text{HbO}_2 \) concentrations (\( \mu \text{M} \)), \( r \) is the distance between the source and detector, and \( \text{DPF} \) is the differential path length factor indicating the lengthening of the average optical path length due to light scattering in tissue. Therefore, by measuring the changes of optical densities at two wavelengths, the changes of \( \text{Hb} \) and \( \text{HbO}_2 \) concentrations can be calculated as:

\[ \Delta \text{Hb} = A \cdot \Delta \text{OD}(\lambda_1) - B \cdot \Delta \text{OD}(\lambda_2), \]
\[ \Delta \text{HbO}_2 = -C \cdot \Delta \text{OD}(\lambda_1) + D \cdot \Delta \text{OD}(\lambda_2), \]

where \( A, B, C, \) and \( D \) are constant coefficients based on the molar extinction coefficients at the respective wavelengths.

The instrument used for prefrontal scanning was a LED-based imager (LEDi, NIM Incorporated, Philadelphia, Pennsylvania).

The system had a flexible probe to match the contour of the human forehead. The probe consisted of four LED diodes as light sources, and photodiodes as detectors that were symmetrically arranged in an area of 3.5 \( \times \) 14 cm\(^2\), conducting to 16 nearest source-detector pairs (i.e., channels) at 2.5-cm separation (see Fig. 1(a)). During the experiment, a Velcro band held the probe firmly on the forehead, and extended from ear to ear in axial direction and from hairline to eyebrow in a sagittal direction (see Fig. 1(b)). The optically probed area should cover approximately the anterior PFC, a part of the dorsolateral PFC, and a part of the ventrolateral PFC. The four LEDS flashed in sequence; the reflected light from the brain was detected with the nearest photodiodes of each LED and converted into digital signals using an analog-digital converter (ADC) card in the control box. Then the digital data were sent to a laptop computer through a serial port. The sampling rate across all 16 channels was 3 Hz.

### 2.3 Data Screening and Analysis

Data screening and analysis were done using Matlab 6.5 (The Mathworks, Natick, Massachusetts). The data were processed for each individual test and analyzed channel by channel for 16 channels. The major factor to be considered in data processing was the physiological noises, which have received increasing attention in recent studies. Besides the functional activation at the cortex, the fNIRS signals also comprise various oscillations related to the spontaneous physiological activities. The most pronounced spontaneous oscillation stems from the cardiac pulsation at about 1 to 2 Hz. It is a very fast oscillation compared to the functional activation and can be filtered out directly. In the lower frequency range, three standard frequency bands were defined:

1. the high frequency (HF) oscillation related to respiration, having a broad peak at the respiratory rate of around 0.3 Hz;
2. the low frequency (LF) oscillation at about 0.1 Hz resulting from vasomotion; and
3. the very low frequency (VLF) oscillation between 0.02 and 0.04 Hz. Little is known about the physiological interpretation of VLF oscillation. The magnitude of the physiological noises can be much bigger than that resulting from the functional activation, because these noises are systemic and embedded in both the cortex and overlying tissues. The physiological noises are implicated in two different aspects: first, the spontaneous oscillations are distinctive characteristics of in-vivo optical reflectance. In data screening, we used a continuous wavelet transform (CWT) algorithm to decompose and examine these spontaneous oscillations to exclude the invalid data that usually resulted from poor probe contact on the scalp. Second, the HF, LF, and VLF oscillations could induce significant aliasing into data analysis, since they have very similar temporal characteristics to the functional activation. A practical strategy to reduce the physiological noises is to perform task-related averaging, since these noises are not temporally correlated. Two steps were followed during the data processing.

1. Data screening: a wavelet transform is a variable-scale representation of signal with a wavelet function that is called a mother wavelet. The wavelet transform of a discrete signal \( x(n) \) is the convolution of \( x(n) \) with a scaled and translated mother wavelet \( \psi(n) \):

\[ C_{a,k} = \sum_{n=1}^{N} x(n) \psi \left[ \frac{n-k}{\alpha} \right], \]

where \( \alpha \) is the scale factor, \( k \) is the translational factor, and \( C_{a,k} \) are wavelet coefficients. Briefly, by altering the scale factor \( \alpha \), the wavelet transform provides a decomposition of the signal at a certain frequency band. In this study, the fourth derivative of Gaussian function was used as the mother wavelet (see Fig. 2(a)). Normalized wavelet coefficients at integer scale \( \alpha = 5, 15, \) and 50 were adopted to represent HF, LF, and VLF oscillations, respectively (see Table 1). If the LED probe contacted the scalp firmly and the reflected light from the brain was acquired properly, continual and systematic oscillations across all channels would be seen clearly after CWT decomposition. For instance, Figs. 2(b)–2(e) show such a segment of undecomposed cerebral data (\( \Delta \text{OD} \), \( \lambda_2=850 \text{ nm} \)) as well as its decomposed VLF, LF, and HF components, respectively. If some channels were in poor contact with the scalp during the test, the decomposed components in these channels were significantly asynchronous to the other channels, and frequently discontinued due to the motion artifacts. Conse-
3 Results

Among the six female subjects, three subjects (subjects 1 to 3) chose a six-letter anagram, and the other three (subjects 4 to 6) chose a four-letter anagram. After data screening, the number of valid tests for each subject is shown in Table 2. The accuracy of their performance ranged from 61.4 to 72.0%, which did not show significant dependence on the difficulty level (six- or four-letter anagram) that they chose.

![Fig. 3](https://nanolithography.spiedigitallibrary.org/journals/Journal-of-Biomedical-Optics/images/3_results.png)

The histograms of task duration from two subjects: (a) subject 3 choosing the six-letter anagram; and (b) subject 4 choosing the four-letter anagram. The bar width in each histogram is 3 sec. For each subject, task durations apparently obey the exponential distribution.

Table 1 The pseudofrequency and 3-dB passband of CWT at scale \( \alpha = 5, 15, \) and \( 50. \)

<table>
<thead>
<tr>
<th>( \alpha )</th>
<th>5</th>
<th>15</th>
<th>50</th>
</tr>
</thead>
<tbody>
<tr>
<td>( f_p ) (Hz)</td>
<td>0.30</td>
<td>0.10</td>
<td>0.03</td>
</tr>
<tr>
<td>Passband (Hz)</td>
<td>0.21 to 0.37</td>
<td>0.07 to 0.12</td>
<td>0.03 to 0.04</td>
</tr>
</tbody>
</table>

Fig. 2 (a) The fourth derivative of the Gaussian function as the mother wavelet in CWT; (b) the undecomposed, cerebral signal (ordinate: channel number); and (c) to (e) the decomposed CWT components at scale factor \( \alpha = 50, 15, \) and \( 5, \) corresponding to the VLF, LF, and HF spontaneous oscillations. Continual and systematic spontaneous oscillations across all channels are observed with good probe contact on the scalp.
Two histograms of anagram duration from subjects 3 and 4 are shown in Figs. 3a and 3b, respectively, demonstrating that each individual’s histogram is commonly more concentrated on the left side, apparently having the exponential distribution. Some extremely long durations are observed from each subject, meaning that the corresponding tasks might be too difficult to solve and subsequently excluded from data analysis. The mean duration for each subject (as given in Table 2) showed significant dependence of duration on the difficulty level: subjects 1 to 3 having the six-letter anagram did take much more time to complete the tasks than subjects 4 to 6 having the four-letter anagram. For subjects 1 to 3, all of D1, D2, and D3 subgroups met the criterions of having seven or more tasks and were selected for data analysis. However, for subjects 4 to 6 in the four-letter anagram group, only subgroups of D1 and D2 were adopted for data analysis, since the D3 subgroup did not have enough anagram tasks (<7 tasks) as we predefined (see Table 3).

### 3.1 Temporal Characterization

For the subgroups with the same task durations, similar hemodynamic patterns due to solving the anagram tasks were observed across the subjects. We selected the most active channels (see the next section to know how to determine this selection) on the left and right sides of the dorsolateral PFC from each subject, as listed in Table 3. Then, we plotted Figs. 4a–4c to show the grand-averaged time courses of $\Delta[HbO_2]$ and $\Delta[Hb]$ (mean $\pm$ SD, N=3) with task durations of D1 to D3, respectively. The data were taken from subjects 1 to 3 who performed six-letter anagrams. A transient “calm” period about 2 to 3 sec after the anagram onset ($t=0$ sec) was observed in all the subgroups, followed by a significant deactivation in the cortex as $\Delta[HbO_2]$ decreased and $\Delta[Hb]$ increased. This deactivation maintained a little longer in the subgroups having longer task duration. Then both $\Delta[HbO_2]$ and $\Delta[Hb]$ gradually recovered, eventually reaching a distinct overshoot in $\Delta[HbO_2]$ and undershoot in $\Delta[Hb]$ in all three subgroups. Moreover, the overall variation of $\Delta[HbO_2]$ was always bigger than that of $\Delta[Hb]$ in the same subgroup. Similarly, Figs. 4d and 4e show the grand-averaged time courses of $\Delta[HbO_2]$ and $\Delta[Hb]$ (mean $\pm$ SD, N=3) with task durations of D1 and D2, respectively, which were from subjects 4 to 6 who performed four-letter anagrams. A reduced deactivation, as compared to the respective subgroups with six-letter anagrams, was also observed in $\Delta[HbO_2]$ and $\Delta[Hb]$.

### 3.2 Spatial Characterization

To investigate the spatial patterns of PFC response, pseudocolor topographies of $\Delta[HbO_2]$ and $\Delta[Hb]$ in the probing area are created based on the hemodynamic data taken from 16 channels. Figure 5 shows the PFC topographic series of $\Delta[HbO_2]$ with a 3-sec interval, ranging from 0 to 18 sec.

### Table 2 The performance of six subjects having valid tests.

<table>
<thead>
<tr>
<th>Subject number</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
</tr>
</thead>
<tbody>
<tr>
<td>n-letter anagram</td>
<td>6</td>
<td>6</td>
<td>6</td>
<td>4</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>Number of tests</td>
<td>13</td>
<td>15</td>
<td>10</td>
<td>6</td>
<td>8</td>
<td>7</td>
</tr>
<tr>
<td>Number of tasks</td>
<td>130</td>
<td>150</td>
<td>100</td>
<td>60</td>
<td>80</td>
<td>70</td>
</tr>
<tr>
<td>Accuracy (%)</td>
<td>70.0</td>
<td>70.0</td>
<td>72.0</td>
<td>70.0</td>
<td>67.5</td>
<td>61.4</td>
</tr>
<tr>
<td>Mean executing time (s)</td>
<td>31.6</td>
<td>24.6</td>
<td>15.0</td>
<td>3.4</td>
<td>8.5</td>
<td>3.5</td>
</tr>
</tbody>
</table>

### Table 3 The number of tasks completed within durations D1 = 2.0 ± 0.3 sec, D2 = 4.0 ± 0.7 sec, and D3 = 8.0 ± 1.0 sec and most active channels in each adopted subgroup for six subjects.

<table>
<thead>
<tr>
<th>Subject number</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of tasks completed within D1</td>
<td>9</td>
<td>11</td>
<td>7</td>
<td>12</td>
<td>14</td>
<td>9</td>
</tr>
<tr>
<td>Most active channel</td>
<td>3,13</td>
<td>5,11</td>
<td>3,13,16</td>
<td>3,11,16</td>
<td>3,11,16</td>
<td>3,13</td>
</tr>
<tr>
<td>Number of tasks completed within D2</td>
<td>19</td>
<td>18</td>
<td>7</td>
<td>20</td>
<td>9</td>
<td>22</td>
</tr>
<tr>
<td>Most active channel</td>
<td>3,13</td>
<td>5,11</td>
<td>3,13,16</td>
<td>3,11,16</td>
<td>3,11,16</td>
<td>3,13</td>
</tr>
<tr>
<td>Number of tasks completed within D1</td>
<td>10</td>
<td>7</td>
<td>9</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Most active channel</td>
<td>3,13</td>
<td>5,11</td>
<td>3,13</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
associated with an anagram task (0 sec represents the onset of task). Data were taken from subject 2, with the task duration of D3 = 8.0 ± 0.7 sec. Each hexagon in the graphs corresponds to the reading from the respective channel at the same location, with its color scale proportional to the temporal value at the given times. As shown in this set of figures, the maximum deactivations (the second and third frames of Fig. 5) were seen at channels 5 and 11 that were located on the left and right dorsolateral PFC, respectively, followed by big overshooting increases approximately occurring in the neighboring regions.

For each individual subgroup with different task durations, the most active channels during execution of the anagrams were determined based on the peak-to-peak amplitude of Δ[HbO2] variation, i.e., the height from P1 to P2 as indicated in Fig. 4(a). For instance, Figs. 6(a)–6(c) show the PFC topographies based on the peak-to-peak amplitudes taken from subject 2 across three duration subgroups (D1 to D3). Channels 5 and 11 in the dorsolateral PFC consistently are the most active channels. Similar and consistent results were also observed from other subjects, as listed in Table 3. Such results clearly demonstrate that each subject kept a consistent pattern to solve the anagram tasks through the tests, activating the same brain regions in the PFC regardless of different durations spent on each task. Interindividual comparison showed that dorsolateral PFC (channels 3 and 5 on the left, and channels 11 and 13 on the right side of PFC) was the region most frequently engaged in anagram tasks. Furthermore, the overall spatial trends obtained at the two difficulty levels (four- and six-letter anagrams) show a similar pattern, while the most active channels slightly differ in amplitude from subject to subject. Therefore, it appears that this functional segregation

![Graphs showing temporal profiles of Δ[HbO2] and Δ[Hb] for different task durations.](image-url)
depends mainly on the characteristics of the individual subject.

3.3 Test of the Superposition Principle

If the brain activation in response to certain stimulation follows a linear system model, the hemodynamic response to a long-duration task \( f(x_1 + x_2) \) can be predicted by the summation of the responses to several shorter tasks \( f(x_1) \) and \( f(x_2) \), based on the principle of superposition: namely, \( f(x_1 + x_2) = f(x_1) + f(x_2) \), where \( x_1 \) and \( x_2 \) represent two time durations and \( f(x) \) denotes the function of hemodynamic response. Assuming that the cognitive load is statistically constant, or has constant amplitude, for all the anagram tasks at the same difficulty level, the test of superposition was performed to examine if the brain activation in response to anagram tasks in the PFC is linear. The data taken from the six- and four-letter anagram groups were analyzed separately, and only the most active channels in dorsolateral PFC were used, as given in Table 3.

In the six-letter anagram group, the first test for superposition was to use the response with a task duration of \( D_1 = 2.0 \pm 0.3 \) sec to predict the response with a duration of \( D_2 = 4.0 \pm 0.7 \) sec. To do so, the hemodynamic signals of \( \Delta[HbO_2] \) and \( \Delta[Hb] \) with a duration of \( D_1 \) were shifted by 2 sec and then added to the original signals to predict the signals with a task duration of \( D_2 \) [see Fig. 7(a)]. Figures 7(c) and 7(d) are generated in this way and clearly show that the added results of \( \Delta[HbO_2] \) and \( \Delta[Hb] \) overpredict the actual...
respective measured signals, meaning that the superposition principle is not valid for the measured signals \( \Delta[HbO_2] \) and \( \Delta[Hb] \) if the shorter stimulation signals of 2 sec are used for prediction. Close inspection on the predicted and measured signals, as expressed by the maximum \( \Delta[HbO_2] \) decrease and maximum \( \Delta[Hb] \) increase after anagram task \( [A_p, \Delta_p, \Delta] \) as seen in Figs. 7(c) and 7(d), also reveals that the predicted signals are approximately 52 and 32% larger than the actual measured signals in \( \Delta[HbO_2] \) and \( \Delta[Hb] \), respectively.

In the second test for linearity, the hemodynamic signals of \( \Delta[HbO_2] \) and \( \Delta[Hb] \) with the duration of \( D = 0 \pm 1 \) sec were predicted using both duration subgroups of D1 and D2, respectively [see Fig. 7(b)]. As shown in Figs. 7(e) and 7(f), the predictions using subgroup D1 are much larger than the measured signals, having approximately 114 and 88% over-prediction in \( \Delta[HbO_2] \) and \( \Delta[Hb] \) amplitude, respectively. The predictions using subgroup D2 approach much closer to the measured signals, as shown in Figs. 7(g) and 7(h), having only about 52 and 18% over-prediction in \( \Delta[HbO_2] \) and \( \Delta[Hb] \), respectively. This means that the hemodynamic signals at the PFC are highly nonlinear when the task duration is shorter than 4 sec, but tend dramatically to be linear if the task duration is longer than 4 sec.

Similar superposition tests were performed in the four-letter anagram group. In this case the hemodynamic signals with D1 duration were used to predict the signals with D2 duration [see Fig. 7(a)]. Figure 8(a) shows 25% over-prediction in \( \Delta[HbO_2] \) amplitude, while the predicted time course in \( \Delta[Hb] \) matched well with the measured signal, as shown in Fig. 8(b). The latter means that the nonlinear effect is not obvious in \( \Delta[Hb] \). It is not surprising since \( \Delta[Hb] \) signals are often weaker than \( \Delta[HbO_2] \) signals, so \( \Delta[Hb] \) could be more easily subject to and suffering from physiological noises. The nonlinear effects shown in \( \Delta[HbO_2] \) signals are expected to be more reliable than those in \( \Delta[Hb] \).

4 Discussion

In this study we have investigated the temporal and spatial variability of hemodynamic responses i.e., \( \Delta[HbO_2] \) and \( \Delta[Hb] \), in the PFC of six human subjects during anagram tasks, with respect to different durations and difficulty levels. From temporal evolution, we observed early deactivation in the PFC as \( \Delta[HbO_2] \) decreased and \( \Delta[Hb] \) increased after the task onset; both \( \Delta[HbO_2] \) and \( \Delta[Hb] \) maintained for some time before returning to the baseline, followed by an overshoot in \( \Delta[HbO_2] \) and an undershoot in \( \Delta[Hb] \). It appears that the early decrease in \( \Delta[HbO_2] \) is affected by the task difficulty level: the PFC response caused by the six-letter anagram shows a bigger, longer decrease than that caused by the four-letter anagram under the same task duration.

From spatial segregation, the dorsolateral PFC near the locations of channels 3 and 5 on the left forehead and channels 11 and 13 on the right forehead show predominant signals during the anagram tasks. This is expected, since the dorsolateral PFC is believed to be specialized for active manipulation and monitoring of information in verbal tasks. The slight variation between channels 3 and 5 as well as between channels 11 and 13 across subjects is believed to result from the individual head size. For some of the subjects, channel 16 at the right ventrolateral PFC showed stronger deactivation than channels 11 and 13; this observation is also reasonable, since the brain area under channel 16 is frequently involved in verbal tasks. Moreover, within each individual subject, good consistency in spatial segregations across different duration subgroups (D1, D2, and D3) is observed.

In this study, the principle of superposition among three subgroups has been specifically tested. The three durations were used to apply the principle of superposition to measured data, i.e., we wish to examine whether the hemodynamic responses will be doubled or tripled if the stimulation periods are doubled or tripled. Our data analysis from both the four- and six-letter anagrams has clearly shown a nonlinear behavior in hemodynamic signals in the PFC with the task durations shorter than 4 sec. The nonlinear behavior in \( HbO_2 \) is more robust than that in \( Hb \). To our current knowledge, this is the first investigation on the nonlinearity of cognitive response based on the principle of superposition. Our finding is complementary to the previous fMRI studies on the nonlinear rate effects in cognitive cortices based on the principle of scaling.

Although fNIRS and fMRI measure similar cortical hemodynamics, several factors need to be further considered while comparing the nonlinear phenomena between the two technologies. First, the spatial resolution of fNIRS is relatively crude and is mainly determined by the measurement density of the optode array being in the range of centimeters in human brain studies. Since the sampling volume in fNIRS is much bigger than the voxel size in fMRI, the nonlinearity observed in fNIRS might be equivalent to that obtained through multi-voxel averaging in BOLD signals at the corresponding cortical areas. Second, fNIRS is more sensitive to the hemodynamic signals in small vessels (i.e., arterioles, venules, and capillaries). Given the strength of the static magnetic field, in contrast, the BOLD signals in fMRI may be associated primarily with large vessels and particularly draining veins. Therefore, a simultaneous comparison of nonlinearity between fNIRS signals and BOLD signal in fMRI has potential to better understand the nonlinear effect of cerebral hemodynamics at both micro- and macrovascular levels.

Studying and understanding nonlinearity of hemodynamic responses to specific stimuli is significant for optimizing experimental designs and data analysis. In general, it is believed
that a longer or stronger stimulation signal will lead to a bigger hemodynamic response. However, this statement may not be completely true if the individual trials are spaced too closely, with fast-rate activation, due to the existence of non-linearity. Large nonlinearities could result in misleading conclusions when using very short intervals between experimental stimuli. Recognizing the appropriate temporal range when the nonlinearity presents will help design better experiments and improve the sensitivity of measurements, as demonstrated in the field of fMRI.\(^{18}\)

Another important reason to study nonlinearity is our attempt to study neural activities to be derived from hemodynamic measurements. Since fNIRS measures changes in hemoglobin concentrations in the brain, this technique does not directly detect any neural or neuronal activities. We expect that nonlinearity study may allow us to extrapolate or explore neural parameters in the following way. When a nonlinear pattern is detected with multiple stimulation durations in such a way as we showed earlier, one can mathematically model a neural adaption function and fit the model to the experimental response functions. A set of fitted parameters can then be obtained to reflect neural activities. Such approaches have been made by an fMRI study\(^{46}\) and adapted in our recent fNIRS investigation.\(^{47}\) While our expectation needs to be further confirmed, we believe that a good understanding of nonlinearity in fNIRS signals will permit the exploration of neuronal activities based on hemodynamic signals.

One noticeable observation in our study is the significant, early decreases in anagram response. The deactivations have maintained about 10 sec after the anagram task started and seem very unlikely to result from the initial dip,\(^ {18,48}\) which results mainly from a temporary lack of oxygen in the activated brain area, being caused by a rapid increase in neural activities. To date, such a decrease in cerebral blood flow and oxygenation, i.e., the negative BOLD response (NBR), has been frequently observed and reported in the fMRI field,\(^ {41,49–51}\) while NBR is opposite to the conventional thought that the brain activation leads to an increase in regional blood flow and oxygenation. The physiological origin of NBR is still an open question and has not been fully understood.

Several explanations for NBR have been given in a variety of fMRI studies using different brain stimulation protocols: one interpretation was associated to the passive hemodynamic changes around the activated brain area, reflecting an effect of blood draining from the neighboring areas, a so-called “blood steal.”\(^ {49}\) Another interpretation against blood stealing was reported in a study of the visual cortex,\(^ {52}\) suggesting that NBR resulted from an active, attention-related suppression of neural activity. Indeed, NBR has been frequently observed in dorsolateral PFC during versatile video-game-like tasks;\(^ {53–55}\) similar to the latter protocols, several fNIRS studies have further confirmed sustained decreases in HbO\(_2\).\(^ {56–58}\) To compare all of these reported studies with NBR, there was little in common except that all the tasks required a response to certain visual stimuli. Such visual stimuli exist in our anagram tasks. We hypothesize that the dorsolateral PFC deactivation in our study results from attention-related suppression, because manipulating or reordering the letters in an anagram requires sustained visual attention. However, we cannot completely rule out the possibility of blood steal based on our fNIRS results, because the probe size in our study was not able to cover the entire dorsolateral PFC.

Given all possible interpretations and hypothesis as discussed, a more recent animal study brings another view\(^ {51}\) that negative BOLD signals do not necessarily mean decreased neuronal activity, but can stem from increased neuronal activity. NBR highly depends on the interaction and balance between hemodynamics and metabolism. Such a conclusion indicates the complexity and uncertainty on how to interpret NBR, which is still under current research exploration in the fMRI field. Similarly, a better understanding on the decrease in HbO\(_2\) signals seen in our anagram study needs to be further explored, while such PFC hemodynamic deactivation is unambiguously observed and in good agreement with multiple fMRI\(^ {51–53}\) and fNIRS\(^ {54–56}\) studies.

## 5 Conclusion

In this study, we wish to prove our hypothesis that nonlinearity between short-term anagram tasks and corresponding hemodynamic responses can be observed by fNIRS at the PFC. With duration-variable anagram tasks, we observe a significant hemodynamic deactivation, as Δ[HbO\(_2\)] decreases and Δ[Hb] increases, during and shortly after the task executions. By using the superposition principle of a linear system, we demonstrate clear nonlinearity in hemodynamic responses in the PFC with task durations shorter than 4 sec. This study basically proves that fNIRS can be utilized to observe a nonlinear relationship between the stimulus parameters and the resultant hemodynamic parameters in the PFC when a short-term anagram task is given. The significance of studying nonlinearity by fNIRS is to possibly investigate brain adaptation and to extrapolate neuronal activities from hemodynamic signals, and thus to comprehend further about neurovascular coupling during brain activities. Furthermore, our observation of significant deactivation in early hemodynamic responses in the PFC is in good agreement with previous reports measured with fNIRS, and is analogous to the NBR that has been frequently observed in the fMRI field. While several explanations for NBR exist, understanding the decrease in HbO\(_2\) signals seen in our study remains to be further explored.

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## References


